

Ravindra B. Bapat • Steve J. Kirkland •
K. Manjunatha Prasad • Simo Puntanen
Editors

Combinatorial Matrix Theory and Generalized Inverses of Matrices

 Springer

Editors

Ravindra B. Bapat
Indian Statistical Institute
New Delhi, India

K. Manjunatha Prasad
Manipal University
Manipal, Karnataka, India

Steve J. Kirkland
National University of Ireland Maynooth
Maynooth Co. Kildare
Ireland

Simo Puntanen
University of Tampere
Tampere, Finland

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Foreword

The success of a conference has to be evaluated by the quality of the scientific presentations and the ability of the organizers to publish the proceedings. If this is the yardstick used, I reckon the International Conference on Combinatorial Matrix Theory and Generalized Inverses of Matrices makes the grade easily.

I congratulate the Department of Statistics, Manipal University, on the successful conduct of the conference and the publication of the proceedings.

Manipal, India

Dr. H. Vinod Bhat

Preface

The *International Workshop and Conference on Combinatorial Matrix Theory and Generalized Inverses of Matrices-2012* was organized by the Department of Statistics, Manipal University, Manipal, India. There were more than 100 registered participants for both of the workshop and conference and 22 invited speakers representing 12 nations across the globe. Two-day conference consisted of four plenary sessions. Invited papers and contributed papers were presented in three parallel sessions dedicated, respectively, to the branches of “Combinatorial Matrix Theory,” “Generalized Inverse of Matrices,” and “Matrix Methods for Statistics.” The international workshop and conference on CMTGIM provided a delightful and fruitful opportunity for all Indian and foreign mathematicians and statisticians at all levels of experience to interact in person and exchange ideas.

“Combinatorial Matrix Theory and Generalized Inverses of Matrices” is being published in an attempt to document the recent developments in the areas discussed at the conference. This book contains about 18 research and expository articles from different speakers and their collaborators. Only the selected articles, after the refereeing process, were retained for the inclusion in this volume. A report on the workshop and conference is presented as an appendix, covering narrative photographs and messages from the Pro Vice-Chancellor, Joint Secretary, CSIR, and the Director General, CSO.

New Delhi, India
Maynooth, Ireland
Manipal, India
Tampere, Finland

Ravindra B. Bapat
Steve Kirkland
K. Manjunatha Prasad
Simo Puntanen

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- Bibhas Adhikari, Indian Institute of Technology, Rajasthan, India.
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- Steve Kirkland, National University of Ireland Maynooth, Ireland.
- S.H. Kulkarni, Indian Institute of Technology Madras, Chennai, India.
- Saroj Malik, Hindu College, University of Delhi, Delhi, India.
- Simo Puntanen, University of Tampere, Finland.
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- Tarkeshwar Singh, Birla Institute of Technology, Goa, India.
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Our sincere thanks are also due to the National Board of Higher Mathematics (NBHM), the Central Statistics Office (CSO) Ministry of Statistics and Programme Implementation, the Council of Scientific and Industrial Research (CSIR), and the International Center for Theoretical Physics (ICTP) for their financial support.

Assistance of K.S. Mohana, Santhi Sheela and M. Vinay in compiling this volume was incredible, and we proudly applaud their effort.

Finally, we thank the team at Springer for their cooperation at all stages of publishing this volume.

September 2012

Ravindra B. Bapat
Steve Kirkland
K. Manjunatha Prasad
Simo Puntanen

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Editors

Ravindra B. Bapat is a Professor at the Indian Statistical Institute, Delhi Centre. He is a Fellow of the Indian Academy of Sciences, Indian National Science Academy and a J.C. Bose Fellow. He served as the President of the Indian Mathematical Society during 2007–2008. He has been on the editorial boards of *Linear and Multilinear Algebra*, *Electronic Journal of Linear Algebra*, *Indian Journal of Pure and Applied Mathematics* and *Kerala Mathematical Association Bulletin*.

Steve J. Kirkland is a Stokes Professor at the National University of Ireland Maynooth. He is currently the Editor-in-Chief of the *Journal Linear and Multilinear Algebra*, and serves on the editorial boards of *Linear Algebra and its Applications*, the *Electronic Journal of Linear Algebra*, and *SIAM Review*. He is also the President of the *International Linear Algebra Society*.

K. Manjunatha Prasad is a Professor of Mathematics at the Department of Statistics, Manipal University, Manipal. He has several publications in the area of his research interest. His research interests are in matrix theory, generalized inverses, ring theory, projective modules and matrices in graph theory.

Simo Puntanen earned his Ph.D. in Statistics from the University of Tampere (Finland) in 1987, where he is presently a Docent and Lecturer of Statistics. He was a Senior Fellow at the Academy of Finland (autumn 1988 and 1993–1995), an Associate Professor at Tampere University during 1997–1998 and worked as a Senior Scientist of the Academy in 1998–1999. He is currently the book review editor of the *International Statistical Review*.

Contributors

Adel Alahmedi Department of Mathematics, King Abdulaziz University, Jeddah, SA

Yousef Alkhamees Department of Mathematics, King Saud University, Riyadh, SA

A. Anuradha Department of Mathematics, Bharathidasan University, Tiruchirappalli, India

Oskar Maria Baksalary Faculty of Physics, Adam Mickiewicz University, Poznań, Poland

R. Balakrishnan Department of Mathematics, Bharathidasan University, Tiruchirappalli, India

R.B. Bapat Stat-Math Unit, Indian Statistical Institute, Delhi, New Delhi, India; Indian Statistical Institute, New Delhi, India

K.P.S. Bhaskara Rao Department of Computer Information Systems, Indiana University Northwest, Gary, IN, USA

Francisco Carvalho Unidade Departamental de Matemática e Física, Instituto Politécnico de Tomar, Tomar, Portugal; CMA—Centro de Matemática e Aplicações, Universidade Nova de Lisboa, Caparica, Portugal

Ka Lok Chu Dawson College, Montreal, Quebec, Canada

K.P. Deepesh Department of Mathematics, Indian Institute of Technology Madras, Chennai, India

Huaian Diao School of Mathematics and Statistics & Key Laboratory of Applied Statistics of MOE, Northeast Normal University, Chang Chun, P.R. China

Jan Hauke Institute of Socio-Economic Geography and Spatial Planning, Adam Mickiewicz University, Poznań, Poland

S.K. Jain Department of Mathematics, King Abdulaziz University, Jeddah, SA; Ohio University, Athens, OH, USA

Sachindranath Jayaraman School of Mathematics, IISER Thiruvananthapuram, Thiruvananthapuram, Kerala, India

Shani Jose Department of Mathematics, Indian Institute of Technology Madras, Chennai, India

Debajit Kalita Department of Mathematical Sciences, Tezpur University, Sonitpur, Assam, India

Tõnu Kollo Institute of Mathematical Statistics, University of Tartu, Tartu, Estonia

S.H. Kulkarni Department of Mathematics, Indian Institute of Technology Madras, Chennai, India

K. Manjunatha Prasad Department of Statistics, Manipal University, Manipal, India; Department of Statistics, Manipal University, Manipal, Karnataka, India

Augustyn Markiewicz Department of Mathematical and Statistical Methods, Poznań University of Life Sciences, Poznań, Poland

AR. Meenakshi Annamalai University, Annamalainagar, India

João Tiago Mexia CMA—Centro de Matemática e Aplicações, Universidade Nova de Lisboa, Caparica, Portugal; Departamento de Matemática, Faculdade Ciências e Tecnologia, Universidade Nova de Lisboa, Caparica, Portugal

K.S. Mohana Department of Statistics, Manipal University, Manipal, India; Department of Mathematics, Manipal Institute of Technology, Manipal, India

M.T. Nair Department of Mathematics, Indian Institute of Technology Madras, Chennai, India

Simo Puntanen School of Information Sciences, University of Tampere, Tampere, Finland

Y. Santhi Sheela Department of Statistics, Manipal University, Manipal, India

Anne Selart Institute of Mathematical Statistics, University of Tartu, Tartu, Estonia

K.C. Sivakumar Department of Mathematics, Indian Institute of Technology Madras, Chennai, India

Sivaramkrishnan Sivasubramanian Department of Mathematics, Indian Institute of Technology, Bombay, Mumbai, India

Murali K. Srinivasan Department of Mathematics, Indian Institute of Technology Bombay, Mumbai, India

George P.H. Styan Department of Mathematics and Statistics, McGill University, Montreal, Quebec, Canada

G. Sudhakara Department of Mathematics, Manipal Institute of Technology, Manipal, India

H.S. Sujatha Department of Mathematics, Manipal Institute of Technology, Manipal, India

Götz Trenkler Department of Statistics, Dortmund University of Technology, Dortmund, Germany

M. Vinay Department of Mathematics, Manipal Institute of Technology, Manipal, India

Helle Visk Department of Public Health, University of Tartu, Tartu, Estonia

Yimin Wei School of Mathematical Science and Key Laboratory of Mathematics for Nonlinear Sciences (Fudan University), Ministry of Education, Fudan University, Shanghai, P.R. China